Comparison of midvelocity fragment formation with projectilelike decay

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The characteristics of intermediate mass fragments (IMFs: 3 ≤ Z ≤ 20) produced in midperipheral and central collisions are compared. We compare IMFs detected at midvelocity with those evaporated from the excited projectilelike fragment (PLF∗). On average, the IMFs produced at midvelocity are larger in atomic number, exhibit broader transverse velocity distributions, and are more neutron rich as compared to IMFs evaporated from the PLF∗. These characteristics of midvelocity fragments are consistent with the low-density formation of the fragments. We present in the different kinematical regions studied, the ⟨E⊥⟩ for isotopically identified IMFs. For a given Z, ⟨E⊥⟩ is either constant or decreases slightly with increasing A, in contradiction with a mass-dependent collective expansion in which all IMFs are emitted on average at the same time. Neutron-deficient isotopes of even Z elements manifest higher kinetic energies than heavier isotopes of the same element for both PLF∗ and midvelocity emission. This result may be because of the charged-particle decay of long-lived excited states.

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I. INTRODUCTION

Cluster emission from nuclear matter can arise from a wide range of phenomena, such as statistical evaporation from normal density nuclear matter at modest excitation [1] or the multifragmentation of low-density nuclear matter at high excitation induced by GeV hadronic projectiles [2]. Collision of two heavy ions at intermediate energies (25 MeV ≤ E/A ≤ 100 MeV) also results in copious intermediate mass fragment (IMF : 3 ≤ Z ≤ 20) production [3,4]. Considerable attention has been focused on understanding the conditions governing the maximum fragment yield [5,6] and the characteristics of the fragments produced [7,8]. In peripheral collisions of two intermediate-energy (20 ≤ E/A ≤ 100 MeV) heavy nuclei (A ∼ 100) a dissipative binary collision occurs resulting in the formation of an excited projectilelike fragment (PLF∗) and targetlike fragment (TLF∗). The dominant IMF yield in such collisions is observed at velocities intermediate between the deexcited PLF∗ and TLF∗ and is not attributable to the standard statistical decay of either of the two reaction partners [9,10]. The IMFs in this kinematical region are referred to as midvelocity IMFs. For more central collisions, the distinctive binary nature of the collision is no longer apparent, nevertheless most of the IMF emission occurs in the same kinematical region as in more peripheral collisions. Although for more peripheral collisions, the dynamical nature of midvelocity fragments has been shown [11–14], in the case of central collisions, statistical approaches are generally used to understand the fragment production [15–17].

On general grounds, the size, composition, and kinetic energies of the observed clusters, apart from their yield, can be related to the composition and excitation of the disintegrating system. For example, the composition of fragments, namely their neutron-to-proton ratio, may provide information on the N/Z of the disintegrating system [18,19]. Several experiments have established the neutron enrichment of IMFs and light clusters (Z ≤ 2) at midvelocity [16,17,20,21]. The observation of neutron-rich fragments in this kinematic region has been interpreted as the N/Z fractionation of hot nuclear material into a neutron-rich gas and a proton-rich liquid [17]. As with any claim of “enrichment” of a quantity, it is necessary to establish the appropriate reference with respect to which the enrichment occurs. We propose that the most appropriate reference for investigating possible enrichment of midrapidity fragments is the N/Z of the emitted fragments from near normal density nuclear matter.

In this work, we examine the fragment characteristics largely independent of the probability of their formation. We show that, at midvelocity, the fragment characteristics manifest significant differences as compared to those evaporated from near normal density nuclear matter. In contrast to previous results [16], the size of the emitting system is shown to not be the determining factor in the composition of the emitted fragments.
To investigate the factors influencing fragment composition, we measured IMF and light charged-particle (LCP; 1 ≤ Z ≤ 2) emission in the reaction $^{114}$Cd + $^{92}$Mo at $E/A = 50$ MeV. We examine midperipheral collisions in which the survival of a well-defined projectilelike fragment occurs. Emission from the PLF* (which presumably is at near normal density) provides a suitable reference for understanding midvelocity IMF emission in the same collisions. We subsequently compare midvelocity IMFs associated with midperipheral collisions and those associated with central collisions.

II. EXPERIMENTAL SETUP

Charged-particles produced in the reaction $^{114}$Cd + $^{92}$Mo at $E/A = 50$ MeV were detected in an exclusive 4π setup. Peripheral collisions were selected by the detection of forward-moving projectilelike fragments (PLFs). These PLFs were detected in the angular range $2.1^\circ \leq \theta^{lab} \leq 4.2^\circ$ and were identified in an annular Si(IP)/CsI(Tl)/PD ring detector (RD) by the $\Delta E$-E technique. This telescope provided elemental identification with better than unit Z resolution for Z ≤ 48, as shown in Fig. 1. The peak at $Z = 48$ corresponds to quasielastically scattered projectile nuclei associated with the most peripheral collisions. The silicon $\Delta E$ element of this telescope was segmented into 16 concentric rings on its junction side and 16 pie-shaped sectors on its ohmic surface. The ring segmentation provided a good measurement of the polar angle of the PLF, typically $\Delta \theta^{lab} < 0.2^\circ$, whereas the pie-shaped sectors allowed a measure of the azimuthal angle [12]. Careful calibration of the CsI(Tl) crystals with the pie-shaped sectors allowed a measure of the azimuthal angle $\phi$. From the measured Z, angle, and energy, the velocity of the PLF was calculated by assigning the $A$ for a given $Z$ consistent with systematics [22] adjusted near $Z_{beam}$ to correspond to the $N/Z$ of the projectile [23]. Intermediate mass fragments with $Z ≤ 9$ and light charged-particles were isotopically identified in the angular range $7^\circ \leq \theta^{lab} \leq 58^\circ$ with the high resolution silicon-strip array LASSA [24,25]. Each of the nine telescopes in this array consisted of a stack of three elements, two ion-implanted, passivated silicon strip detectors (Si(IP)) backed by a 2 × 2 arrangement of CsI(Tl) crystals each with photodiode readout. The second silicon of each telescope was segmented into 16 vertical strips and 16 horizontal strips, resulting in good angular resolution ($\Delta \theta^{lab} \approx 0.43^\circ$). The nine LASSA telescopes were arranged in a 3 × 3 array, the center of which was located at a polar angle $\theta^{lab} = 32^\circ$ with respect to the beam axis. The energy threshold of LASSA is 2 and 4 MeV/A for $\alpha$ particles and carbon fragments, respectively. A typical example of the isotopic resolution achieved by LASSA is shown in Fig. 2. Isotopes of Li and Be are clearly resolved with an energy resolution of $\approx 2-5\%$. To augment the limited kinematical coverage of LASSA and the RD, the low-threshold Miniball/Miniwall array [26] was used to identify charged-particles emitted in the range $5^\circ \leq \theta^{lab} \leq 168^\circ$. Using pulse-shape discrimination, particles detected in the Miniball/Miniwall array were isotopically identified for $Z ≤ 2$.

III. GENERAL REACTION CHARACTERISTICS AND EVENT SELECTION

We begin by examining midperipheral (MP) events distinguished by the survival of a projectilelike fragment at forward angles. To examine these peripheral collisions we have selected events in which a heavy PLF with $30 ≤ Z ≤ 46$ is detected in the RD ($2.1^\circ \leq \theta^{lab} \leq 4.2^\circ$) coincident with at least three charged-particles in the Miniball/Miniwall array. This latter charged-particle requirement suppresses the most peripheral collisions and results in the associated multiplicity distribution shown in Fig. 3(a). These MP collisions are characterized by an average total charged-particle multiplicity, $\langle N_C \rangle$, of

FIG. 1. Element distribution measured by the ring detector for the angular range $2.1^\circ \leq \theta^{lab} \leq 4.2^\circ$. The arrow indicates the atomic number of the beam.

FIG. 2. Isotopic resolution achieved in LASSA for isotopes of Li and Be. The spectra have been summed over all nine LASSA telescopes.

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distribution of fragments detected in the RD. For central collisions \( \langle N_C \rangle \geq 20; \langle N_C \rangle = 21.8; \mu_2 = 1.89 \) the ridge centered near the projectile velocity is no longer observed, as shown in Fig. 4(b). The observation that a clear Coulomb circle does not exist has traditionally been interpreted as evidence that the collision is no longer a binary process. However, the observation of a large charged-particle multiplicity together with the absence of a Coulomb circle does not preclude the existence of a dissipative binary process. Rather, these observations can be reconciled with the rapid deexcitation of the PLF* and TLF* on a time scale commensurate with their reseparation. In contrast to the well-defined Coulomb circle of Fig. 4(a), the emission pattern for central collisions is broad and featureless with substantial emission near the center-of-mass velocity. In these collisions we deduce from the charged-particle multiplicity that \( b/b_{\text{max}} = 0.26 \), from which we estimate \( Z_{\text{source}} \approx 72 \) [30].

The charged-particle multiplicity has often been used in this manner to select central collisions. Examination of the \( Z \) collisions studied, we have determined that \( \langle Z_{\text{PLF}} \rangle \approx 41 \). Also clearly evident in Fig. 4(a), and well established by earlier work [9,10], is that considerable fragment emission occurs at midvelocity—emission not originating from the isotropic statistical decay of the PLF* or TLF* reaction partners [11]. For the remainder of this work we define midvelocity fragments as those with \( 0 \leq V_\parallel \leq 1 \) cm/ns in the center-of-mass frame.

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![FIG. 3. (a) Charged-particle multiplicity distribution associated with the detection of a PLF with \( 30 \leq Z \leq 46 \) in the RD; (b) velocity distribution for \( 30 \leq Z \leq 46 \) detected in RD; (c) atomic number distribution of fragments detected in the RD.](image)

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![FIG. 4. (Color online) Invariant cross-section plots of the emission of \( ^6 \)Li fragments in the center-of-mass frame. (a) Associated with \( 30 \leq Z_{\text{PLF}} \leq 46 \). (b) Associated with \( N_C \geq 20 \). The dashed arrow indicates \( V_{\text{PLF}}^\parallel \) while the solid arrow indicates \( V_{\text{BEAM}} \). The differential yield is presented on a logarithmic scale.](image)
distribution of the largest measured particle in the RD associated with these events, however, is quite revealing. As evident in Fig. 5(a), although the largest probabilities are associated with either the detection of no fragment \((Z = 0)\) or a helium in the RD, there is a significant probability of detecting a large fragment with \(Z > 10\) in the RD. (It should be noted that the triggering threshold in the RD was set to not trigger on hydrogen nuclei resulting in a measured yield of zero for \(Z = 1\) in Fig. 5(a).) This detection of a large fragment \((Z > 10)\) occurs even though a large charged-particle multiplicity has been required. This result is consistent with the physical picture of a large overlap of projectile and target nuclei which still results in a binary exit channel with survival of a projectilelike and targetlike fragment. The cumulative yield associated with such events, \(\Sigma P(Z_{\text{RD}})\), is shown in Fig. 5(b) where

\[
\Sigma P(Z_{\text{RD}}) = \int_{Z_{\text{RD}, \text{max}}}^{Z_{\text{max}}} \frac{dN}{dZ_{\text{RD}, \text{max}}} dZ.
\]  

(1)

Evident in Fig. 5(b) is the result that \(\Sigma P(Z_{\text{RD}}) \approx 0.1\) for \(Z_{\text{RD}, \text{max}} = 10\). This result reveals that \(\approx 10\%\) of the collisions selected simply by the requirement that \(N_c \geq 20\) are in fact associated with binary collisions. Because of the limited angular acceptance of the RD, the probability of binary dissipative collisions for the multiplicity selection used might be somewhat higher.

Further evidence that these events are associated with a binary exit channel and not simply an anisotropic emission pattern is provided in Fig. 6. In this figure, we examine the correlation between the atomic number and the velocity of these fragments detected in the RD. With the exception of the lightest fragments \((Z \leq 3)\), the fragments detected in the RD have a most probable velocity (indicated by the points) that is slightly damped from the beam velocity (indicated by the arrow). For \(Z > 9\) the most probable velocity of the PLF is 3.1 cm/ns, corresponding to a damping of \(\approx 1.3\) cm/ns of the beam velocity. This inclusion of binary dissipative events even for the large multiplicity selection does not significantly affect any of our subsequent analysis.

IV. ELEMENTAL YIELDS

The \(Z\) distribution for IMFs associated with MP and central (Cent) collisions for both PLF* emission and emission at midvelocity is shown in Fig. 7. The observed yields in each case have been normalized for the range \(3 \leq Z \leq 8\). To understand the \(Z\) distribution at midvelocity \((0 \leq V_{||} \leq 1\) cm/ns), we use PLF* emission (solid circles) as a reference. Fragments emitted from the PLF* were selected on the basis of their emission angle, \(\theta_{\text{PLF}}\), in the PLF frame \((85^{\circ} \leq \theta_{\text{PLF}} \leq 95^{\circ})\). This angle was determined on an event-by-event basis. For these same MP collisions, the \(Z\) distribution at midvelocity (open triangles) exhibits a suppression of yield for lighter IMFs \((Z = 3\) and 4) and an enhanced production of heavier IMFs \((Z \geq 5)\) as compared to PLF* emission (solid circles). This increase of the relative production of heavier IMFs at the expense of lighter IMFs is even larger for the case of central collisions (open squares). We conclude therefore that at midvelocity (both in midperipheral and central collisions), heavier fragments are produced at the expense of lighter fragments, as compared to PLF* emission.

This change in the \(Z\) distribution at midvelocity when compared to PLF* emission, can be understood within a statistical framework. Within such a framework, the \(Z\) distribution is influenced by the excitation, density, and size of the disintegrating system. Statistical emission of a fragment is governed by an effective emission barrier relative to
FIG. 7. Z distribution of fragments associated with midperipheral collisions emitted in the angular range $85^\circ \leq \theta_{PLF} \leq 95^\circ$ in the PLF frame (solid circles); midperipheral collisions and at midvelocity (open triangles); and fragments associated with central collisions at midvelocity (open squares). The lines depict the Z distribution predicted by the statistical model GEMINI (see text for details). The yield for each case has been normalized to unity for the interval shown.

the temperature of the emitting system. Increased relative probability for the emission of heavy fragments, can thus reflect either a reduction in this effective barrier and/or an increase in the temperature of the system. A reduction in the density of the emitting system naturally results in a reduction of the effective barrier. The Z distribution of midvelocity fragments in midperipheral collisions is intermediate between that of PLF* emission and emission associated with central collisions. From this observation one may conclude that within a statistical interpretation, the relative “energy cost” has already begun to change from that of the PLF*. At midvelocity, the enhancement of yield for $Z \geq 6$ in the central case as compared to MP collisions may be because of the influence of finite source size. For MP collisions, the small size of the fragmenting system ($Z_{source} \approx 21$) at midvelocity may limit the production of heavy IMFs.

FIG. 8. Distributions of $V_\perp$, for $^7$Be and $^{10}$Be fragments in the center-of-mass frame. (a) Midperipheral collisions and $80^\circ \leq \theta_{PLF} \leq 100^\circ$; (b) midperipheral collisions and $0 \leq V_\parallel \leq 1$ cm/ns; (c) central collisions and $0 \leq V_\parallel \leq 1$ cm/ns. All distributions have been normalized to unity. neutron-rich $^{10}$Be at low $V_\perp$ is larger than that of neutron-deficient $^7$Be. Because of the angular selection used, the constraints of the experimental angular acceptance do not significantly impact the observed velocity distribution, an expectation confirmed by Coulomb trajectory calculations subsequently discussed. In contrast to the peaked distributions in Fig. 8(a), the distributions associated with midvelocity

V. TRANSVERSE VELOCITY DISTRIBUTIONS

We present in Figs. 8 and 9 the transverse-velocity distributions of $^7$, $^{10}$Be and $^6$, $^9$Li fragments. The different distributions correspond to fragments observed in different kinematical regions for midperipheral and central collisions. Depicted in Fig. 8(a) is the transverse-velocity distribution of $^7$Be and $^{10}$Be fragments that are emitted with $80^\circ \leq \theta_{PLF} \leq 100^\circ$ in the PLF frame. Based on Fig. 4(a) we understand these fragments as being emitted from the PLF*. In this case, peaked distributions are observed as is expected from the Coulomb “ring” observed in Fig. 4(a), indicative of a well-defined Coulomb barrier characteristic of surface emission. The relative probability of

FIG. 9. Distributions of $V_\perp$, for $^6$Li and $^9$Li fragments in the center-of-mass frame. (a) Midperipheral collisions and $80^\circ \leq \theta_{PLF} \leq 100^\circ$; (b) midperipheral collisions and $0 \leq V_\parallel \leq 1$ cm/ns; (c) central collisions and $0 \leq V_\parallel \leq 1$ cm/ns. All distributions have been normalized to unity.

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emission for midperipheral collisions [Fig. 8(b)] are essentially flat. This flatness of the \( V_\perp \) distribution is particularly observed for \(^{10}\text{Be} \) and \( V_\perp \leq 2.5 \text{ cm/ns} \). The observation of large yield for low \( V_\perp \) indicates the absence of significant Coulomb repulsion in the transverse direction. Therefore, the observed \( V_\perp \) distributions reflect principally the initial \( V_\perp \) distributions. A broad and relatively flat initial \( V_\perp \) distribution is compatible with a neck-fragmentation scenario [31] or a Goldhaber picture in which the midvelocity zone results from abrasion/ablation of nucleons between projectile and target nuclei followed by coalescence [32,33]. The difference in the tails of the \( V_\perp \) distribution between PLF\(^*\) emission and midvelocity emission may be interpreted as the midvelocity source having a higher initial temperature than the PLF\(^*\) or possibly reflect the Fermi motion of the abraded nucleons.

Displayed in Fig. 8(c) are the \( V_\perp \) distributions for fragments emitted at midvelocity in central collisions. These distributions also manifest broad peaks and high velocity tails similar to those observed in Fig. 8(b). Close examination, however, reveals that in this case the \( V_\perp \) distribution is more peaked than in Fig. 8(b), suggesting that the Coulomb repulsion is larger in magnitude. This hypothesis is qualitatively consistent with the larger size (atomic number) of the source at midvelocity for central collisions in contrast to midperipheral collisions. Conversely, the peak for the central case is broader than for the case of PLF\(^*\) emission shown in Fig. 8(a), possibly indicating the volume breakup of a low-density source [34] or surface emission from a hot nucleus as it expands [35].

A semi-quantitative description of the \( V_\perp \) distributions presented in Fig. 8 can be achieved by comparing the experimental data with a N-body Coulomb trajectory model that simulates the superposition of multiple source emission. In this model, all emission was assumed to be surface emission originating from either the PLF\(^*\) or a midvelocity source. The characteristics of the PLF\(^*\) were taken from the \( Z \) and energy directly measured, assuming the PLF\(^*\) had the \( N/Z \) of the projectile. Event by event we assumed the \( Z \) of the midvelocity source to be \( Z_{\text{midvelocity}} = Z_{\text{system}} - Z_{\text{PLF}}(1 + Z_T/Z_P) \). We determined \( Z_{\text{midvelocity}} \approx 21 \). Each source also has an associated temperature that is varied independently. The two sources were separated by an initial distance of 30 fm and were allowed to emit isotropically. Our use of surface emission in the midvelocity case for midperipheral collisions simply provides an ansatz for performing the simulation and should not be interpreted as a physical description in this case. This particular choice of surface emission in the model notably affects the low-velocity region of the transverse-velocity spectrum.

Although a volume emission scenario results in a broader distribution, the shape of the spectrum in the high velocity region is largely unchanged.

This simple Coulomb model with \( T_{\text{PLF}} = 7 \text{ MeV} \) provides a reasonable description of the PLF\(^*\) emission as shown in Fig. 8a by the lines. As the fragments selected are emitted with \( \theta_{\text{PLF}} \approx 90^\circ \), it is difficult to associate the excess in the tail of the \(^7\text{Be} \) distribution as compared to this thermal model with pre-equilibrium fragment emission processes. This excess above the prediction of the simple thermal model will be subsequently examined. As thermal energy is the only source of initial kinetic energy in the model, even with \( T_{\text{midvelocity}} = 20 \text{ MeV} \) we underestimate the tails of the \( V_\perp \) spectra depicted in Fig. 8(b). The physical origin of such a high temperature is unclear. The simulation also indicates that the contribution of TLF\(^*\) emission to the midvelocity region examined is insignificant. Analysis of the \( V_\perp \) distributions for Li isotopes reveals similar spectral shapes and slope parameters (\( T_{\text{PLF}} = 7 \text{ MeV} \) and \( T_{\text{midvelocity}} = 20 \text{ MeV} \)) as shown in Fig. 9. Kinetic "temperatures" of similar magnitude have been previously reported for midvelocity IMF emissions [13,36].

It is noteworthy that both the \(^7\text{Be} \) and \(^{10}\text{Be} \), as well as the \(^{6,9}\text{Li} \), spectra associated with midvelocity emission, shown in Figs. 8 and 9, require a large initial kinetic energy (\( T_{\text{midvelocity}} = 20 \text{ MeV} \)). The enhanced probability of low \( V_\perp \) emission as compared to the surface emission model may reflect temperature-dependent surface-entropy effects [37] or a transition from surface to volume emission [2].

**VI. ISOTOPIC COMPOSITION**

By integrating the yields over the entire range of \( V_\perp \) observed, we construct the following ratio:

\[
R = \frac{Y(\text{42Z})}{Y(\text{41Z})}.
\]

The value of \( R(\text{10Be}/\text{7Be}) \) for PLF\(^*\) emission is 1.15, whereas at midrapidity it is considerably higher, 2.2 for midperipheral collisions and 2.25 for central collisions. Based on these integrated yields, one observes that for Be,

\[
\frac{R(\text{midvelocity, midperipheral})}{R(\text{PLF, midperipheral})} = \frac{2.2}{1.15} = 1.91, \quad (3)
\]

whereas

\[
\frac{R(\text{midvelocity, central})}{R(\text{PLF, midperipheral})} = \frac{2.25}{1.15} = 1.96 \quad (4)
\]

Thus, the integrated yield of \(^{10}\text{Be}^*/^{7}\text{Be} \) at midvelocity for midperipheral and central collisions is comparable and significantly different from PLF\(^*\) emission. The behavior exhibited by the \( Y(\text{10Be})/Y(\text{7Be}) \) is also observed for \( Y(\text{3Li})/Y(\text{6Li}) \). At midrapidity the value of \( R(\text{3Li}/\text{6Li}) \) is 0.21 for midperipheral collisions and 0.26 for central collisions, whereas for PLF\(^*\) emission it is 0.13. For both midperipheral and central collisions, the \( Z \) distributions, transverse-velocity distributions, and fragment composition at midvelocity differ markedly from PLF\(^*\) emission.

It is important to consider whether the observed \( N/Z \) enrichment at midvelocity is influenced by the Coulomb field of the PLF\(^*\). Radial repulsion of fragments from the PLF\(^*\) results in \(^7\text{Be} \) fragments displaced more toward midvelocity than \(^{10}\text{Be} \) fragments. Therefore the Coulomb field of the PLF\(^*\) and TLF\(^*\) can lead to an increase in the yield of neutron-deficient isotopes at midvelocity. Hence, because of these qualitative arguments the primordial \( N/Z \) composition at midvelocity may be higher than that experimentally observed.

To assess these Coulomb field effects, we have used the N-body Coulomb trajectory model previously described. The relative emission probability for the PLF\(^*\)
within a surface emission picture the temperature of the source must be somewhat higher. Thus, the GEMINI calculations and emission from the PLF∗ dependence) will require accounting for the anisotropic emission, we deduce an excitation of \( E^∗ / A \) to be 2.11. The distortion, particularly important for low \( V_\perp \), depends on the IMF emission rates relative to the PLF∗-TLF∗ reseparation and is beyond the scope of the present analysis.

**VII. GEMINI CALCULATIONS**

To understand the PLF∗ decay better, we performed calculations with the statistical-model code GEMINI [39], which describes surface emission from an excited nucleus including emission from excited states and their sequential decay. We examined the isotopic yields as a function of the excitation and spin of a parent nucleus. At each excitation energy we roughly reproduce the average atomic number of the measured PLF∗. In Table I, for a fixed \( J = 0h \) we observe that the \( Y(10Be)/Y(7Be) \) decreases with increasing \( E^∗ / A \), whereas for fixed \( E^∗ / A \), it increases with increasing \( J \). For \( J = 0h \) to reproduce the measured value of 1.15 associated with PLF∗ emission, we deduce an excitation of \( E^∗ / A \approx 3–4 \text{ MeV} \). As the level density is taken to be \( a = A / 9 \text{ MeV}^{-1} \) in the model, this excitation corresponds to a temperature of \( T \approx 6 \text{ MeV} \), in reasonable agreement with the tails of the transverse-velocity distribution. If the PLF∗ has significant spin \( (\approx 20h) \), the temperature of the source must be somewhat higher. Thus, within a surface emission picture the \( Y(10Be)/Y(7Be) \) and the transverse-velocity distributions constrain the excitation and spin of the emitting source. Correctly accounting for the interplay of both of these quantities is necessary to describe the conditions of the emitting source. For these conditions \( (Z = 48, A = 114, E^∗ / A = 3.5 \text{ MeV}, J = 0h) \), we have compared the yield distribution of fragments predicted by GEMINI with that observed for PLF∗ emission. The solid line shown in Fig. 7 is the GEMINI yield distribution normalized to the range \( 3 \leq Z \leq 8 \). Although in general the agreement between the GEMINI calculations and emission from the PLF∗ is reasonable, GEMINI overpredicts the relative yield of \( Z = 3 \) and underpredicts the relative yield for \( Z > 4 \).

<table>
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<th>( E^∗ / A (\text{MeV}) )</th>
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<th>( J = 20h )</th>
<th>( J = 40h )</th>
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**TABLE I. Results of GEMINI calculations indicating the dependence of \( Y(10Be)/Y(7Be) \) on excitation energy, \( E^∗ / A \), and spin, \( J \), for emission from the PLF∗ \( (Z \approx 40–48, N/Z \approx 1.375) \).**

**VIII. Z AND A DEPENDENCE OF \( \langle E_\perp \rangle \)**

The average transverse energies of \( 2 \leq Z \leq 6 \) fragments are displayed in Fig. 10 for different impact parameter and velocity selection criteria. To examine emission from the PLF∗ without being biased by the minimum angular acceptance of LASSA, we have selected emission for \( 85^o < \theta^{PLF} < 95^o \) in the PLF frame. The values of \( \langle E_\perp \rangle \) for these different selections can be understood in the context of a simple physical picture in which fragments acquire their transverse kinetic energy as a result of Coulomb repulsion, thermal motion, and possibly energy associated with collective expansion [41]. As the thermal component is mass (Z) independent, an observed Z dependence can be attributed to Coulomb repulsion of fragments from the emitting PLF∗ or the presence of collective motion [41]. Distinguishing between the Z and A dependence of the \( \langle E_\perp \rangle \) can differentiate between the Coulomb and collective contributions to the transverse energy. In the case of emission from the PLF∗ (solid circles), the measured average transverse kinetic energies in the PLF frame generally increase with Z. The magnitude of \( \langle E_\perp \rangle \) for \( Z = 2 \) is roughly consistent with values previously reported for a similar system [42]. These measured magnitudes of \( \langle E_\perp \rangle \) can be understood within a surface emission picture in which fragments are emitted from the surface of a hot nucleus. The \( \langle E \rangle \) in such a picture is given by \( \langle E \rangle = \langle V_C \rangle + 2 \langle T \rangle \) where the Coulomb energy \( V_C = 1.44 (Z_{PLF}^2 - Z_{fragment}^2) Z_{fragment} / R \) with \( R \), the center-to-center separation distance between the fragment and the PLF, taken as \( R = 1.2 [(A_{PLF} - A_{fragment})^{1/3} + A_{fragment}^{1/3}] + 2 \text{ fm} \). The average Coulomb energy has been calculated within this simple picture. The corresponding \( \langle E_\perp \rangle \) \( \approx \langle E \rangle / 2 \) for a temperature of \( T = 7 \text{ MeV} \) is indicated by the solid line in Fig. 10, whereas \( T = 9 \text{ MeV} \) is represented by the dotted line. The magnitude of the observed \( \langle E_\perp \rangle \) and the dependence on Z is qualitatively described by this simple picture, bolstering the view that this emission is standard statistical emission from a near normal density PLF∗.

In Fig. 10, a marked contrast between emission from the PLF∗ and fragments at midvelocity associated with midperipheral collisions (open triangles) is observed. For midperipheral collisions, the \( \langle E_\perp \rangle \) of midvelocity fragments is affected by the choice of frame because of the transverse
momentum of the PLF*. To eliminate the impact of this collective motion in midperipheral events, we examine \( \langle E_\perp \rangle \) in the PLF frame. In this frame, midvelocity fragments in MP collisions manifest significantly lower \( \langle E_\perp \rangle \) and for \( 3 \leq Z \leq 6 \) essentially no dependence of \( \langle E_\perp \rangle \) on \( Z \) exists. The \( \langle E_\perp \rangle \) for helium is approximately 25–30% lower than for IMFs. The magnitude of \( \langle E_\perp \rangle \) for \( 3 \leq Z \leq 6 \) is \( \approx 22 \text{ MeV} \), essentially 2/3 of the Fermi energy. The magnitude of \( \langle E_\perp \rangle \) for \( Z = 2 \) is \( \approx 16 \text{ MeV} \). \( \langle E_\perp \rangle \) values of similar magnitude at midvelocity have previously been reported for IMFs, integrated over \( Z \), and neutron-rich light charged-particles for a significantly lighter system [43]. This independence on \( Z \), together with the fact that the \( \langle E_\perp \rangle \) is approximately 2/3 the Fermi energy suggests that the transverse energy of these fragments does not contain any significant Coulomb contribution, as was previously conjectured based on the \( V_\perp \) distribution shown in Figs. 8 and 9. This result is consistent with a physical picture in which fragments aggregate in a dilute nuclear medium—compatible with a Goldhaber scenario as has been previously suggested [36]. Both the \( Z \) independence of \( \langle E_\perp \rangle \) and the reported magnitudes in the present work are consistent with those previously reported [36]. Alternatively, this behavior can be viewed as the volume breakup of a low-density source or as emission from a distended configuration. On the basis of transverse energies, it has been proposed [13,36] that fragments intermediate between the PLF* and TLF* are dynamical in nature, maintaining early-stage correlations of the collision [44]. To disentangle between these different scenarios it may help to examine if this constancy in the transverse energy is manifested for different isotopes of a given element.

For midvelocity fragments associated with central collisions (open squares), examination of the dependence of \( \langle E_\perp \rangle \) on \( Z \), and in particular the magnitudes of the measured \( \langle E_\perp \rangle \), is particularly revealing. For this case, \( \langle E_\perp \rangle \) increases monotonically with \( Z \), indicating a Coulomb influence. For \( Z = 2 \), the value measured in this work is consistent with values previously reported [42]. The magnitude of \( \langle E_\perp \rangle \) is only slightly larger than in the case of emission from the PLF* (solid circles). These two cases, however, involve significantly different charge associated with the emitting system. For central collisions the initial atomic number of the midvelocity source is almost double that of the PLF* \( (Z_s = 72 \text{ as compared to } Z_{\text{PLF}^*} = 41) \). Hence, the similarity of the values of \( \langle E_\perp \rangle \) for central collisions with those for emission from the PLF* suggests that for central collisions, fragments originate either from a dilute nuclear system (either volume breakup or surface emission during expansion) or after considerable charge has been removed from the system by fast light charged particle emission. The large Coulomb barrier for IMF emission favors early emission of IMFs making IMF emission following light charged particle deexcitation, on average, less likely.

To disentangle the contributions of Coulomb energy and any possible collective flow [41] to the \( \langle E_\perp \rangle \), we examine the dependence of \( \langle E_\perp \rangle \) on \( A \) for individual elements in Fig. 11. Significant collective expansion effects have been previously asserted [15,45], particularly for the case of central collisions. Evident in Fig. 11(a) for central collisions, in the case of \( N > Z \), the observed \( \langle E_\perp \rangle \) for IMFs does not increase with increasing \( A \) for a given \( Z \) but is either constant or decreases slightly. This observation contradicts the expectation of a mass-dependent collective flow, at least in the transverse direction. The most striking feature of Fig. 11(a) is that neutron-deficient isotopes, particularly \(^3\text{He}, ^7\text{Be}, \text{ and } ^{11}\text{C}\), exhibit larger \( \langle E_\perp \rangle \) than other isotopes of the same element.

**FIG. 10.** Average transverse energies for \( 2 \leq Z \leq 6 \) selected under different criteria. For the PLF*, fragments were selected in the angular range \( 85^\circ \leq \theta_{\text{PLF}} \leq 95^\circ \), whereas midvelocity fragments have \( 0 \leq V_\perp \leq 1 \text{ cm/ns} \) in the center-of-mass frame.

**FIG. 11.** Average transverse energies as a function of mass number for \( 2 \leq Z \leq 6 \) for midperipheral and central collisions with different selection criteria. For the PLF*, fragments were selected in the angular range \( 85^\circ \leq \theta_{\text{PLF}} \leq 95^\circ \), whereas midvelocity fragments have \( 0 \leq V_\perp \leq 1 \text{ cm/ns} \) in the center-of-mass frame.
For $^6\text{Li}$ essentially no enhancement is observed, whereas for $^{10}\text{B}$ only a modest enhancement is observed. One possible reason for this difference between odd and even $Z$ is that only for even-$Z$ are nuclides with $N < Z$ observed with significant yield. An enhancement in the average energy of $^3\text{He}$ and $^7\text{Be}$ has previously been reported in inclusive measurements of 5.5 GeV protons on uranium where this observation was related to a higher temperature or larger deposition energy associated with these emissions [46]. This enhancement in the kinetic energy of neutron-deficient fragments in comparison to other isotopes of the same element has also been observed in an exclusive experiment for central collisions in the system $^{112}\text{Sn} + ^{112}\text{Sn}$ at $E/A = 50$ MeV and has been interpreted as evidence for surface emission from a hot, expanding nuclear system [47]. It has been hypothesized that the larger kinetic energy observed for the neutron-deficient isotopes originates because they are emitted on average earlier than other isotopes of the same element [47].

In contrast to the previous work that focused solely on central collisions [47], we also present the dependence of $\langle E_\perp \rangle$ associated with midperipheral collisions for both emission from the PLF$^*$ and the midvelocity regime. In the case of midvelocity, shown in Fig. 11(b), we observe the same effect as for central collisions, although the magnitude of the enhancement is somewhat less. As the physical picture of a hot source that emits as it expands is not compatible with the case of midvelocity emission for midperipheral collisions, the observed trend must have an alternate explanation. In the case of emission from the PLF$^*$ [Fig. 11(c)], $^{11}\text{C}$ does not show an enhancement in contrast to the two midvelocity cases, emphasizing the difference between midvelocity fragment production and emission from the PLF$^*$. A significant enhancement of the average kinetic energy is still observed for $^3\text{He}$ and $^7\text{Be}$ emitted from the PLF$^*$. Thus, this kinetic enhancement of neutron-deficient isotopes is not associated simply with central collisions in which a low density, expanded source may be formed, but also occurs in the standard statistical decay of a near normal density PLF$^*$. A difference of $\approx 2$ MeV is observed between the $^3\text{He}$ and $^4\text{He}$ average kinetic energies. Because of the low excitation energy of this system, sequential feeding of $^3\text{He}$ is expected to be negligible. Consequently, the observed energy difference between $^3\text{He}$ and $^4\text{He}$ can be largely attributed to the earlier average emission time of $^3\text{He}$ as compared to $^4\text{He}$. This difference provides a reference point for the increase in cluster kinetic energy because of differences in the average emission time. The large difference observed in average kinetic energies of neutron-deficient isotopes in the $^{114}\text{Cd} + ^{92}\text{Mo}$ system is therefore not principally because of differences in the average emission time of fragments.

Direct evidence that the excitation of the emitting source is primarily responsible for the enhancement of the neutron-deficient isotopes is presented in Fig. 13 for emission from the PLF$^*$. In Fig. 13(a) the $\langle E_\perp \rangle$ for isotopes of helium are shown as a function of the PLF velocity. For this portion of the analysis we expand our definition of the PLF to include $15 \leq Z_{\text{PLF}} \leq 46$ [29]. It has previously been demonstrated that the velocity damping of the PLF$^*$ is associated with the excitation incurred in the PLF$^*$ following the interaction phase of the collision [29]. The deduced excitation energy scale is indicated at the top of the figure, and the beam velocity is represented by an arrow. As $V_{\text{PLF}}$ decreases from the beam velocity (excitation energy increases) the $\langle E_\perp \rangle$ for $^3\text{He}$, $^4\text{He}$, and $^6\text{He}$ all increase monotonically. To explore the differences between the increase in kinetic energy for the different helium isotopes in a more sensitive manner, we examined the increase in the $\langle E_\perp \rangle$ for $^3\text{He}$ and $^4\text{He}$ relative to $^6\text{He}$. These results are presented in the lower panel of Fig. 13. The difference in transverse energy between $^3\text{He}$ and $^4\text{He}$ increases with increasing excitation from 5.7 MeV at $\langle E^*/A \rangle \approx 2$ MeV to 9.3 MeV at $\langle E^*/A \rangle \approx 5.8$ MeV. Conversely, aside from
an initial decrease, the transverse energy difference between $^6\text{He}$ and $^4\text{He}$ relative remains approximately constant over the measured range. We emphasize that the average kinetic energy enhancement for neutron-deficient isotopes increases with increasing excitation energy (solid stars), opposing the expected behavior based on an emission time displacement argument.

These observations may be qualitatively understood by considering the growing importance of charged-particle decay channels with increasing excitation energy. A fragment emitted from a hot source with an initial thermal energy accelerates in the Coulomb field of the emitting system and acquires its asymptotic kinetic energy. If this fragment decays by neutron emission, the velocity of the secondary fragment is on average the same as the primary fragment at the moment of decay, thus its observed kinetic energy is only impacted by the change in mass. However, should the fragment undergo charged-particle decay, then the kinetic energy observed for the secondary fragment reflects the Coulomb energy acquired by its parent up to the moment of decay, which is larger because of the larger parent atomic number. Only if the lifetime of the parent is sufficiently long for it to transform a significant fraction of its initial Coulomb energy into kinetic energy will the kinetic energy of the daughter fragment be appreciably increased. Instantaneous decay of the parent fragment will not result in an increase in the kinetic energy of the daughter fragments. This physical picture suggests that the neutron-deficient isotopes manifest a secondary decay contribution from relatively long-lived charged-particle channels (i.e., narrow resonances at relatively low excitation in the parent fragment). It is therefore clear from the evidence presented that the fragments are not created relatively cold as predicted in some multifragmentation models [49]. Moreover, these hot fragments do not decay instantaneously. Measurement of the yield associated with multiparticle resonant decay would provide quantitative information about this scenario. Unfortunately, the present experimental data does not allow examination of these resonant decays. With increasing excitation, the secondary decay feeding to $^3\text{He}$ and $^4\text{He}$ changes, presumably affects the yield ratios of the two isotopes, a reference benchmark for isotope thermometry [50,51]. It should be realized that independent of the underlying origin of the kinetic energy difference, there is an inherent danger of examining double ratios such as $[Y(^6\text{He})/Y(^4\text{He})]/[Y(^6\text{Li})/Y(^4\text{Li})]$ involving only one isotope with $N < Z$ that manifests a considerably different kinetic energy. Our results may also suggest that extracting the primordial $N/Z$ to investigate the possible isospin fractionation of a dilute nuclear medium requires detailed measurement of both neutron and charged-particle resonant decays.

**IX. CONCLUSIONS**

In summary, it is revealing to compare the characteristics of midvelocity fragments and those emitted in the deexcitation of a hot, near-normal density nucleus, namely the PLF*. The $Z$ distributions and the transverse-velocity distributions for midvelocity emission are different from those associated with PLF* emission. The integrated yield ratios of $^{10}\text{Be}/^{12}\text{Be}$ and $^6\text{Li}/^8\text{Li}$ reveal that midvelocity and PLF* emission are also substantially different in $N/Z$. For central collisions and midperipheral collisions, these observed yield ratios are enhanced by a factor of approximately two with respect to PLF* emission. In the case of emission from the PLF*, the $Z$ dependence of $\langle E_\perp \rangle$ shows that fragment emission is consistent with standard evaporation from near normal density nuclear matter. In central collisions the $Z$ dependence and magnitude of $\langle E_\perp \rangle$ for midvelocity fragments are inconsistent with normal density formation. For midvelocity fragments formed in midperipheral collisions, the $Z$ independence of $\langle E_\perp \rangle$ and a magnitude of approximately two-thirds of the Fermi energy, suggest cluster formation through coalescence of abraded nucleons. All these facts are consistent with the low-density formation of fragments at midvelocity for both midperipheral and central collisions, indicating that the conditions for fragment formation at midvelocity are significantly different from those of PLF* emission.

In contrast, for all the kinematical regions studied, $\langle E_\perp \rangle$ for IMFs is either constant or decreases slightly with increasing $A$, for a given $Z$. This observation is in contradiction with a mass-dependent collective expansion in which all IMFs are emitted on average at the same time. Examination of $\langle E_\perp \rangle$ for isotopically identified fragments shows that neutron-deficient isotopes, particularly those with $N < Z$, exhibit larger average transverse kinetic energies than heavier isotopes of the same element. This result is observed in all kinematic regions studied both for midperipheral as well as central collisions. Moreover, this enhancement of the kinetic energies for neutron-deficient
isotopes increases with increasing excitation energy. This result suggests that the fragments are produced hot and that long-lived charged-particle decay may be important for $N < Z$ clusters. The magnitude of the enhancement indicates that these decays occur with significant probability and investigating them may shed light on the conditions of fragment formation, motivating the future study of resonant decay.

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